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NEUTRON AND GAMMA RAY PRODUCTION CROSS SECTIONS FOR SILICON

M.R. Bhat, M.D. Goldberg, R.R. Kinsey, A. Prince, H. Takahashi

March 1973

BROOKHAVEN NATIONAL LABORATORY ASSOCIATED UNIVERSITIES, INC. UPTON, NEW YORK 11973



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NATIONAL NEUTRON CROSS SECTION CENTER

BROOKHAVEN NATIONAL LABORATORY ASSOCIATED UNIVERSITIES, INC.

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1. Introduction

This report describes a reevaluation of silicon neutron and photon production cross-sections data by the National Neutron Cross Section Center. This evaluation was finished in Sept. 1972 and it uses all the data available to the authors up to that time.

In order to put this evaluation in its proper perspective, it seems appropriate to present a brief history of this evaluation. The original evaluation of Si was due to M.K. Drake.¹ This evaluation had both neutron and gamma production cross-section files up to 20.0 MeV. These data files were revised by P.G. Young to conform to data format changes, with additional changes in some of the cross-section data in limited energy regions by R.Q. Wright. To the resulting data files M.K. Drake and R.R. Kinsey² added data on $\bar{\mu}_{T}$, ξ , γ and revised the gamma-production cross-section due to capture. They also modified the cross-section for the production of the 1.779 MeV gamma-ray to reflect the changes made by R.Q. Wright in the corresponding inelastic cross-section. This evaluation was later assigned a MAT No. = 1151 and became part of the ENDF/B-III data library. The present evaluation RSIC No. 4151, Mod. 2 is based on this evaluation by Drake and Kinsey with extensive modifications which will be described in detail in the following pages. A brief summary of these changes along with the history of this evaluation is given in a tabular form below. If there is no reference to changes in a specific cross-section in this report, it is to be understood that the corresponding data files are the same as in the ENDF/B-III evaluation.

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History of the Silicon Evaluation

Author	Description and or Revisions	Report
M.K. Drake	Original evaluation with neutron and gamma production files up to 20 MeV	GA-8628 (DASA-2099) May 1, 1968
P.G. Young	Revised for format changes	
R.Q. Wright	<pre>Total and elastic cross-sections revised 1.8-3.62 MeV Added non-elastic cross-section Total inelastic and inelastic cross- section to the 1.779 MeV level revised between 1.85-3.53 MeV Elastic angular distribution given as Legendre coefficients</pre>	
M.K. Drake and R.R. Kinsey	Sections on μ_L , ξ , γ added Gamma production cross-sections due to capture revised Cross-sections for the production of the 1.779 MeV gamma ray by inelastic scattering changed to agree with the corresponding changes in the inelastic scattering cross-section made by R.Q. Wright This Evaluation was given MAT NO = 1151 and is part of the ENDF/B-III Library	ENDF/B Summary Documentation ENDF-201
Authors of this Report	Total cross-section data replaced by new NBS data from 0.5-20 MeV Elastic, non-elastic, total inelastic and partial inelastic cross sections changed to conform to new total cross-section data (n, α) cross-section reevaluated from 8.4- 20.0 MeV $\overline{\mu}_L$, ξ , γ , files changed New Legendre coefficients for elastic and inelastic scattering data added Gamma production cross-sections due to inelastic scattering recalculated Energy distribution of secondary photons recalculated using a statistical model The data files resulting from these modif- ications on the MAT = 1151 evaluation were given an RSIC No. = 4151, Mod 2 and sent to RSIC on Sept. 20, 1972	This Report ENDF-186 BNL-50379 March 1973

2. General Properties of Silicon Isotopes

2.1 <u>Isotopic Mass and Possible Neutron</u> Induced Reactions

Natural silicon is made up of three isotopes - 28 Si, 29 Si and 30 Si. Their fractional abundances and isotopic masses are given in Table 1. One can readily see that the properties of natural silicon are essentially determined by 28 Si. The nuclear masses are from the compilation of Wapstra and Gove.³ In Table 2 we give the Q values for the different possible nuclear reactions up to a maximum neutron energy of 20 MeV. These were also calculated using the same mass tables. Since some of these reactions viz: (n,t), (n, 3 He) and (n,n α) were found to make very small contributions, they were ignored in the evaluated data set. From this Table we note that the Q-value for the (n, α) reaction for a mixture of isotopes should be 33.1 kev whereas in the ENDF/B-III version it is given as 32.7 kev. Since they are so close the Q-value was left unchanged at 32.7 kev. Rest of the (n, particle) data files were not changed.

2.2 Energy Levels of the Silicon Isotopes

The energy levels of the three silicon isotopes, along with their spins and parities, are given in Figs. 1-3. These constitute the result of some of the latest work on the level schemes of these isotopes and is mostly due to the experimental work in Refs. 4-10. The level schemes are essentially the same as used in the original Drake evaluation with a few minor changes in level energies and spin assignments. These level schemes were used in the nuclear model calculations for the different reaction cross-sections to be described later.

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2.3 <u>Discrete Gamma Rays Produced</u> by Neutron Interactions

The discrete gamma rays produced by $(n,n'\gamma)$ reactions in the Si isotopes are also shown in Figs. 1-3. In Tables 3-5 we give a list of these gamma rays along with the initial and final nuclear states and their transition probabilities. This information is taken from the Drake report with a few minor modifications and is due to the data in Refs. 11-23. This data is needed for calculating the gamma production cross-sections due to inelastic scattering as will be described later on.

In Table 6 we give a list of the gamma rays originating from thermal neutron capture in silicon along with their multiplicities. This data is from the work of Spits et. al.,¹⁰ Lycklama et. al.²⁴ and by Blichert-Toft and Tripathi.²⁵ This is the experimental data used to derive the gamma production cross-section due to neutron capture. At higher neutron energies, the experimental data of Lundberg and Bergqvist²⁶ at 68 kev was used.

3. Neutron Cross Sections

3.1. The Total Cross Section

The total neutron cross-section data used in the original Drake and ENDF/B-III evaluations are described in detail in the earlier report.¹ In the present evaluation we have changed the total cross-section data in the energy interval 0.5-20.0 MeV using the NBS data of Schwartz et. al. 27 Another set of total cross-section data of comparable quality is that due to Cierjacks et. al.²⁸ from Karlsruhe. On comparison of these two sets of data, it was found that the Karlsruhe data gave a higher cross-section in general. Thus at 8.7 MeV the Karlsruhe data is 6.8% higher than the NBS data, pointing to some possible problems with background subtraction. Hence, it was decided to use the NBS data which has a statistical error of about 3% at the lower end of the energy scale and about 4% at the higher end. The data points naturally are very closely spaced at the lower end of the energy scale and they become sparser as one goes up in energy. The scatter in the energy points also becomes large at the higher end of the scale and the experimental data does not show any well-defined structure above 12.0 MeV. In order to obtain a smooth curve passing evenly amongst the data points a spline fit was made to the data points using a program SPLIN written by D.E. Cullen.²⁹ In this program one has to specify the abscissa and ordinates of a certain number of nodes to obtain the corresponding spline fit. By trial and error one can determine the nodes needed to have a curve passing through the experimental points and reproduce faithfully the general trend of the experimental data. One result of such a fit is shown in Figs. 4-7 where the curve indicates the total cross-section in the ENDF/B files obtained from the spline fit and the points are the NBS experimental data. Above

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12.0 MeV, because of the large spread in the data, the experimental points were averaged over one MeV energy intervals and the mean value given at the mid-point of the energy range. This essentially gives a constant crosssection without any structure at the high energy end of the scale.

3.2. The (n, α) Cross-Section

The (n, α) cross-section was left unchanged up to 8.4 MeV as given in the ENDF/B-III evaluation. Above this energy it was re-evaluated to conform to some recent experimental data. These changes are discussed in the following.

Above 8.4 MeV, there are no measurements of the (n,α) cross-section for 28 Si. There are, however, some experimental data for the (n,α) cross-section of 30 Si. Hence, use was made of the theoretical calculations of Gardner and Yu³⁰ which give the ratio of the (n,α) cross-sections of 28 Si, 29 Si and 30 Si. These calculations are based on a statistical model and give the relative cross-sections of the isotopes of an element as a function of the incident particle energy, the Q-value of the reaction, the level density and the pairing energy of the daughter nucleus. The ratios of the (n,α) cross-sections for the silicon isotopes at about 14 MeV as calculated by these authors are:

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si: 29 si: 30 si = 1.00:1.27:0.485 .

The experimental values for 30 Si (n, α) cross-section available at the time of the Drake evaluation were: Paul and Clarke³¹ 45.9 ± 25.0 mb at 14.5 MeV; Khurana and Govil³² 123.0 ± 15.0 mb at 14.8 MeV and Pasquarelli³³ 175.0 ± 18.0 mb at 14.7 MeV. Since then, two additional values have been published viz. Ranakumar et. al.³⁴ 68.0 ± 8.0 mb at 14.4 MeV and Singh³⁵ 73.6 ± 10.3 mb at 14.5 MeV. Adopting the two newer values which are in

good agreement, we take a weighted average to give 70.5 mb for the (n,α) cross section of $^{30}\text{Si.}$

If the calculated ratios of Gardner and Yu given above and this value for the (n, α) cross-section for 30 Si are used, one obtains for 28 Si $\sigma(n, \alpha) =$ 145.4 mb and for 29 Si $\sigma(n, \alpha) = 184.6$ mb. However, this result is at variance with the experimental data of Andersson-Lindström 36 who measured 28 Si $\sigma(n, \alpha): {}^{29}$ Si $\sigma(n, \alpha)$ ratio as 8.5 ± 1.2 at 14.5 MeV. Hence, as a way out of this contradiction, it is assumed that Gardner and Yu's theoretical calculations are likely to be more realistic in a comparison between even-even nuclei i.e. 28 Si and 30 Si rather than between even-even and even-odd nuclei i.e. 28 Si and 29 Si. Therefore using the Andersson-Lindström ratio of 8.5 and the 28 Si (n, α) cross-section to be 145.4 mb the corresponding cross-section for 29 Si is found to be 17.1 mb. Thus, one obtains the final values adopted in this evaluation at a nominal energy of 14.5 MeV as: 28 Si $\alpha(n, \alpha) = 145.4$ mb, 29 Si $\alpha(n, \alpha) =$ 17.1 mb and 30 Si $\alpha(n, \alpha) = 70.5$ mb.

These cross-sections weighted with the natural abundances of the respective isotopes give the (n,α) cross-section for natural Si as 137.1 mb at 14.5 MeV. It should be noted here that if the much higher value of 184.6 mb had been adopted for the ²⁹Si (n,α) cross-section as given by the Gardner and Yu ratio, the cross section of silicon would be 145.0 mb. This is only 5.8% higher than 137.1 mb and is well within the uncertainties of the cross-section. The (n,α) cross-section for natural silicon as given in the Drake evaluation¹ is 246.5 mb at 14.5 MeV. The new value adopted in this evaluation is about 44% lower indicating a newer set of cross-section values between 8.4 and 20.0 MeV.

At the time of the previous evaluation, several data sets existed in which measurements were made giving the cross-section versus energy for the

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production of various alpha groups. Since ²⁸Si is the dominant isotope, all the alphas are ascribed to the α_0 , α_1 , α_2etc. groups of this isotope. Such data existed from several separate measurements for neutron energies up to 8.4 MeV. The previous evaluation considered each experiment in detail and provided a composite total alpha production cross-section for ²⁸Si which was then defined as the total (n, α) cross-section for natural silicon from threshold to 8.4 MeV.

Since then, another study of this reaction has been published by Grimes.³⁷ The total elastic (at two angles - 15° and 30°), (n,p_{0+1}) , (n,p_{2+3}) , (n,α_0) , (n,α_1) , (n,α_2) and (n,α_3) cross-sections were measured between 6.64-13.44 MeV. The measurements of the (n,p_1) and (n,α_1) reactions were made simultaneously with a silicon surface barrier detector serving as both the target and the detector. The normalization was thus internal and effectively to the total cross-section. A plot of the sum of (n,α_0) , (n,α_1) , (n,α_2) and (n, α_3) production cross-sections of Grimes between 6.64 and 8.4 MeV when compared to the natural silicon (n,α) cross-section of the Drake evaluation indicates excellent agreement with respect to both the absolute magnitude and the structure of the cross-section.

The structure in the Grimes data continues above 11.0 MeV, but the sum cross-section is no longer the total production cross-section since α_4 , α_5 etc. are not accounted for though clearly seen in the spectra. Thus, at 13.44 MeV the "sum" cross-section value is about 35 mb as compared to the 137.1 mb "best value" at 14.5 MeV recommended in this evaluation. Hence, it is concluded that the (n, α) curve of the previous evaluation still represents adequately the (n, α) cross-section from the threshold to 8.4 MeV.

Using the 207.6 mb value at 8.4 MeV from the previous evaluation and 137.1 mb at 14.5 MeV arrived at in this evaluation, a smooth curve was

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drawn to represent the average natural silicon (n,α) cross-section. This curve rises to a maximum of about 269 mb at about 10.6 MeV. The curve was then continued above 14.5 MeV to 20.0 MeV by a linear extrapolation on a semi-log plot. The ratio of the 14.5 MeV and 20.0 MeV values were made as close as possible to the same ratio of the (n,α_0) reactions as measured by Rubbino and Zubke.³⁸ The resulting curve of the (n,α) cross-section as given in the present evaluation is shown in Fig. 23.

3.3. Inelastic Scattering Cross-Section

Adoption of new total cross-section and (n,α) data as described constitute two of the major changes in the present silicon evaluation as compared to its earlier versions. Since there was no significant new data to warrant extensive changes in the other cross-sections, it was decided to keep the rest of the (n,γ) and (n, particle) cross-sections unchanged. However, the elastic and inelastic scattering cross-sections to the various excited states of the silicon isotopes had to be changed in conformity with changes in the total cross-section. The procedure adopted for such changes is described below.

Nuclear model calculations were made using the ABACUS-2 optical model $code^{39}$ and Greenlees⁴⁰ parameters which are given in Table 7. The level excitation energies and their spins and parities used in these calculations are given in Figs. 1-3. Such calculations give, total, elastic and inelastic scattering cross-sections for the three silicon isotopes. A sum of these calculated total cross-sections weighted according to the isotopic abundance would give us a "total" cross-section containing no (n, particle) cross-sections or the (n, γ) cross-section. Hence, the results of the optical model calculations were normalized by multiplying them by the ratio

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$\frac{\sigma_{\text{Total (expt)}} - \Sigma \sigma_{(n, \text{ particle})} \sigma_{(n, \gamma)}}{\sigma_{\text{"Total" (calc)}}}$

as a function of the neutron energy. In particular, this ratio was used to normalize the inelastic scattering cross-sections to the individual levels in the three isotopes of silicon. These were the first 12 levels in ²⁸Si up to an energy of 8.260 MeV, the first 5 levels in 29 Si up to an energy of 3.623 MeV and the first 4 levels in 30 Si up to an energy of 3.788 MeV. The assumptions underlying such a normalization procedure are firstly that of an extreme compound nucleus picture and secondly that the relative magnitudes of the different inelastic cross-sections are given by the optical model calculations. The result of such a normalization is to obtain a set of inelastic cross-sections to the different excited states with the same kind of fine structure as in the total cross-section "built in". It is interesting to compare these cross-sections with experimental data available for the 1.779, 4.617, 4.975 and 6.276 MeV levels in ²⁸Si. There are no experimental data for the excitation cross-sections to any other levels. As of this writing the most extensive data is for the 1.779 MeV level in ²⁸Si. The experimental data plotted against the normalized curve is shown in Fig. 14 from the threshold to 5.0 MeV and in Fig. 15 from 5.0 to 10.0 MeV. The experimental data is from Refs. 41-51. In such a comparison one must bear in mind the fact that data on inelastic excitation functions is measured with a much broader neutron energy resolution than the total cross-section data. This is indicated by the horizontal error bars about each data point. The vertical bars indicate the error in the value of the cross-section. Where such bars are absent, either these uncertainties have not been quoted by the authors or they are of the order of the size of the corresponding

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symbols. Looking at the trend of the calculated cross-section and the experimental points, the agreement is good except in the case of the 1961 Lind and Day data at low energies which are consistently lower. The high resolution inelastic cross-section data for the 1.779 MeV level from threshold to 3.53 MeV given in Ref. 52 could not be used as it was not available in the final form at the time of the evaluation. In the case of 4.617 MeV level (Fig. 16) a comparison of the available experimental data with the normalized curve indicates that the experimental data are lower by nearly a factor of 2. For the 4.975 and 6.276 MeV levels (Figs. 17 and 18) the agreement between experiment and the evaluated curves is satisfactory.

As mentioned earlier, the inelastic scattering cross-sections for a total of 21 levels in the three isotopes of silicon have been given in the evaluated data files. The remaining inelastic scattering cross-sections to some 46 remaining nuclear levels were lumped together as a cross-section for scattering into the continuum (MF = 3, MT = 91). This cross-section is shown in Fig. 19. It should be mentioned here, as a point of detail, that the energy grid used in normalizing the different partial cross-sections was the same as that used to give the total cross section. This simplifies to a considerable extent the whole procedure and one is assured of an energy grid which is fine enough to accommodate the structure in the different cross-sections.

3.4. The Elastic Scattering Cross-Section

A sum of all the inelastic scattering cross-sections, the (n, particle) cross-sections and the capture cross-section when subtracted from the total cross-section determined from the experimental data gives us the elastic scattering cross-section. It is interesting to compare this cross-section

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with experimental data where available. Such a comparison from 0.5-11.0 MeV is shown in Fig. 8. The experimental data are due to the workers in Refs. 43, 46, 49, 50, 53-56. The horizontal bars associated with each data point indicate the neutron energy resolution and the vertical bars the data errors. The agreement between the experimental data and the evaluated curve is good especially if one bears in mind the broad neutron energy resolution of the individual data points.

4. Angular Distribution of Secondary Neutrons

4.1. Elastically Scattered Neutrons

The angular distributions of the elastically scattered neutrons were given in the original Drake evaluation as normalized probability distributions. These were converted to give the corresponding Legendre polynomial expansion coefficients using the code CHAD.⁵⁷ The experimental data sets used have been tabulated in the original report.¹ In addition, some of the new data by Knitter and Coppola,⁴⁶ Kinney and Perey⁵⁰ were used. The experimental data of the last reference for $E_n = 8.56 \pm 0.08$ MeV and a Legendre polynomial fit of order eight are shown in Fig. 27. A value of about 980 mb/sr was used in the forward direction and between 140° and 180°, the experimental points were supplemented by points read off from the dashed curve given in this reference. In fitting the data for differential elastic scattering, consistency checks with Wick's limit were made. It was also made sure that the Legendre polynomial expansion coefficients reproduced a non-negative differential elastic scattering cross-section.

In addition, new files giving $\bar{\mu}_L$, ξ and γ were generated using the code⁵⁸ DUMMY5 and plots of these are shown in Figs. 24-26.

4.2 Inelastically Scattered Neutrons

The angular distribution of inelastically scattered neutrons for the 1.779 MeV level of ²⁸Si were converted to the corresponding Legendre polynomial expansion coefficients and are included as such in the evaluated data files. In addition to the data in the Drake evaluation, new data by Kinney and Perey⁵⁰ has been used. A fit made to the $E_n = 7.55 \pm 0.04$ MeV and $E_{ex} = 1.779$ MeV data from this reference using CHAD is shown in Fig. 28. It should also be mentioned here that coupled channel calculations were carried out to determine the direct contribution due to the coupling of the first two excited states of each silicon isotope to account for the anisotropy of the differential inelastic scattering. However, since the experimental data showing such anisotropy were sparse, it was decided not to use these calculations.

5. Gamma Ray Production Cross Sections

5.1. Production of Radiative Capture Gamma Rays.

a. Low Energy Capture (10 5 eV - 50 keV)

The energies and multiplicities for the gamma rays due to neutron capture in this energy range were obtained from the thermal neutron capture data of Spits et al.,¹⁰ Lycklama et al.²⁴ and Blichert-Toft and Tripathi.²⁵ These data are given in Table 6, with gamma ray energies, their multiplicities, energy of the initial state as well as the isotopic identification of the target nucleus. The binding energies of neutrons in the compound nuclei resulting from neutron capture in ²⁸Si, ²⁹Si and ³⁰Si are 8,474.2 ± 0.5 kev, 10,609.9 ± 1.0 kev and 6589.1 ± 0.7 kev respectively. However, an effective binding energy of 8,767.6 kev for silicon as recommended by Orphan et. al.⁶⁰ has been used in this evaluation. The experimental data given in Table 6 was therefore normalized to this Q-value for the (n, γ) reaction.

b. High Energy Capture (above 50 kev)

For this neutron energy range, the experimental data of Lundberg and Bergqvist²⁶ at 68 keV are used. The measurements in this work were done with a NaI(T1) scintillator and as such, the gamma ray energies are given with a broader energy resolution as compared to a Ge(Li) detector. By comparison with Ge(Li) detector data of thermal neutron capture, it was possible to establish a plausible one-to-one correspondance between the gamma ray energies given by Lundberg and Bergqvist and the Ge(Li) detector measurements. The multiplicities of the 68 keV measurements were used and if a gamma ray was known to be a primary transition, the kinetic energy of the neutron was added to the gamma-ray energy to satisfy energy conservation. The multiplicities and the gamma ray energies are given starting from 0.1 MeV neutron energy in steps of 0.1 MeV up to 1.0 MeV. Above this neutron energy,

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the gamma spectrum is treated as a continuum and only average multipicities are given in File 12 (MF=102) and the energy distribution of the gamma spectrum is given in File 15. These energy distributions were obtained by putting all the discrete gamma rays in gamma ray energy bands 0.5 MeV wide to give a histogram.

5.2 Cross Sections for the Production of $(n,n'\gamma)$ Gamma Rays

The data on the gamma rays and their transition probabilities given in Tables 3-5 was used to calculate the gamma production cross-section due to inelastic scattering from the corresponding inelastic scattering cross-sections. In these calculations, gamma rays originating from levels less than or equal to the 8.260 Mev level in ²⁸Si, the 3.623 MeV level in ²⁹Si and the 3.788 MeV level in ³⁰Si were explicitly treated as discrete gamma rays and their production cross-sections calculated. Since excited states lying above the three energies in the corresponding isotopes were treated as part of the "continuum"; the gamma rays originating in these levels were treated differently as described below. If the transition probabilities of the different gamma rays are known, it is possible to follow in detail, the number populating a particular state and the number depleting such a population and calculate the gamma production cross-sections. Since, the resulting cross-sections had a lot of fine structure in them, they were averaged over 20 kev intervals from the threshold up to 5.0 Mey, and over 200 kev intervals to 10.0 MeV and over 1.0 Mev intervals up to 20.0 MeV. These cross-sections were calculated up to 20.0 MeV for some of the gamma transitions in $\frac{28}{5}$ si where data on the production cross-section were available at energies above 10.0 Mev; otherwise then cross-sections were calculated only up to 9.0 Mev in ²⁸Si and up to 4.0 MeV in ²⁹Si and ³⁰Si. The

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experimental data on the production cross-sections is due to Tucker et al.⁶¹, Drake et al.⁶² and other experimental data given in Ref. 61. A comparison between the calculated curves and the experimental data is shown in Figs. 29-39. The neutron energy resolution is shown by a horizontal bar, otherwise it is less or equal to the horizontal extension of the symbol. It should be emphasized here that the calculated curves have not been normalized to any experimental value. The agreement between the calculated curves and the experimental data is good, especially for the more intense gamma rays.

The photons not treated as discrete gamma rays were accounted for by assuming that they form part of a continuous gamma spectrum. This is the case with those discrete gamma rays whose cross-sections are given only up to 9.0 MeV. However, cross-sections of some of the more intense gamma rays are given up to 20.0 MeV. Hence, the following procedure (suggested by M.K. Drake) was used to subtract the contributions of the discrete gamma rays. It is assumed that the gamma production cross-section at 9.0 MeV is 1.48b and at 14.5 MeV is 1.75b¹. The ratio of the total gamma production cross-section to the nonelastic cross-section (this is the yield or the multiplicity $y(E_n)$) is found to be 1.23 at 9.0 MeV and 1.60 at 14.5 MeV. It was assumed that a straightline interpolation could be made between 9.0 and 14.5 MeV to obtain this ratio at points in between and that one could extend the straight line to get this ratio up to 20.0 MeV. The recommended non-elastic cross-section multiplied by this ratio thus gives the total gamma production cross-section. The energy distribution of the continuum photons, $\frac{d\sigma\gamma}{dE\gamma}$ ($E_{\gamma} \leftarrow E_{n}$) as well as the average photon energy \overline{E}_{γ} (E_n) averaged over this energy distribution were calculated using the GRØGI-III Code,⁶³ as described in the next section. The total energy released per reaction as photons is \overline{E}_{γ} (E_n) x y (E_n). From this the total

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gamma ray energy E_{γ}^{D} released as discrete photons (this is obtained by averaging $E_{\gamma i}$ for the i-th discrete gamma over its corresponding production cross-section $\sigma_{n,xi}$) is subtracted to give gamma energy E_{γ}^{C} appearing in the continuum. This is used to calculate the photon production cross-section for the continuum as

$$\sigma_{n, x\gamma}^{C} (E_{n}) = \frac{E_{\gamma}^{C}(E_{n})}{E_{\gamma}(E_{n})} \sigma_{n,x}(E_{n})$$

The normalized energy distribution for the continuum is also given in File 15.

5.3 Energy Distribution of the Secondary Gamma Rays

In discussing capture gamma ray spectra it was mentioned how gamma rays due to capture above 1.0 MeV neutron energy were grouped together into bins 0.5 MeV wide and the distribution normalized to give an energy distribution of the gamma ray spectrum.

The gamma-ray production cross-sections, its energy distribution and mean energy were calculated from 9.0 to 20.0 MeV. Neutron energy using the GRØGI-III. Code.⁶³ Since ²⁸Si is the dominant isotope calculations were made only for ²⁸Si. In this code, cascade calculations based on a statistical theory are performed to estimate contributions from the different gamma rays. In these calculations, the level-density formula used is that of Gilbert and Cameron⁶⁴ The level density parameters for the parent nucleus and the different daughter nuclei produced in the cascade processes were all taken from this paper and are listed in Table 8. At high excitation energies involving high nuclear spin values the relative importance of γ versus particle emission has to be properly calculated using the yrast levels. The yrast levels for high spin were calculated using the prescription given in the paper of Gilat⁶⁵ and Grover and Gilat⁶⁶ and the compilation of Endt and Van der Leun¹⁷. These data are given in Table 9 in MeV. The binding energies of neutron, proton and α particles for all nuclei are given in Table 10 in MeV. All data except for
²¹Ne were taken from the previous reference. The data for ²¹Ne are from
Mattauch et al.⁶⁷ The transmission coefficients for n, p and α particles
were calculated using ABACUS-2 using the optical model parameters of
Becchetti and Greenless⁴⁰. The optical model parameters for the α particles
are from Huizenga and Igo⁶⁸. The GRØGI-III Code calculates the gamma spectrum
from each cascade process. The total gamma production cross-section as well
as the energy distribution of the gamma spectrum were obtained by summing all
these contributions.

Acknowledgement

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TABLE 1

Isotope	Fractional Abundance	Isotopic Mass	•
28 _{Si}	0.9221	27.9769286	•
²⁹ Si	0.0470	28.9764969	
30 _{Si}	0.0309	29.9737722	

Properties of the Naturally Occurring Silicon Isotopes

Reaction Q Values for the Silicon Isotopes

	Q Value (MeV)				
Reaction -	28 _{Si}	²⁹ Si	30 _{Si}		
(n,y)	8.4738	10.6098	6.5884		
(n,p)	- 3.8598	- 2.8980	- 7.7574		
(n,np)	-11.5853	-12.3337	-13.507		
(n,d)	- 9.3607	-10.1091	-11.2824		
(n,t)	-16.1610	-11.5769	-14.4612		
(n, ³ He)	-12.1377	-14.1686	-16.2743		
(n,α)	- 2.6529	- 0.0331	- 4.1998		
(n,n α)	- 9.9848	-11.1268	-10.6428		
(n,2n)	- 17.1774	- 8.4738	-10.6097		

TABLE	3
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Initial State		Final S	Final State		m	
Energy (MeV)	_J ۳	Energy (MeV)	_J	E Y (MeV)	Probability (%)	
8.941	2+	1.779	2+	7.162	50.0	
8.941	2+	0.0	0+	8.941	50.0	
8.902	1-	1.779	2+	7.123	100.0	
8.588	3+	6.878	3	1.710	10.0	
8.588	3+	6.276	3*	2.312	10.0	
8.588	3+	1.779	2+	6.809	80.0	
8.543	6+	4.617	4+	3.926	100.0	
8.413	4	6.878	37	1.535	86.0	
8.413	4	6.276	3+	2.137	2.0	
8.413	4	4.617	4*	3.796	4.0	
8.413	4	1.779	2*	6.634	8.0	
8.328	1+	1.779	2+	6.549	45.0	
8.328	1+	0.0	0+	8.328	55.0	
8.260	1-	1.779	2+	6.481	80.0	
8.260	1-	0.0	0+	8.260	20.0	
7.935	2+	1.779	2+	6.156	20.0	
7.935	2+	0.0	0+	7.935	80.0	
7.798	3+	6.276	3+	1.522	25.0	
7.798	3+	1.779	2+	6.019	75.0	
7.416	2+	1.779	2+	5.637	10.0	
7.416	2+	0.0	0+	7.416	90.0	
7.381	1+	1.779	2+	5.602	55.0	
7.381	1*	0.0	0+	7.381	45.0	
6.889	4*	1.779	2+	5.11	100.0	
6.878	3	1.779	2+	5.099	30.0	
6.878	3	0.0	0+	6.878	70.0	
6.691	0+	1.779	2+	4.912	100.0	
6.276	3+	4.617	4+	1.659	10.0	
6.276	3*	1.779	2+	4.497	90.0	
4.975	0.	1.779	2*	3.196	100.0	
4.617	4 ⁺	1.779	2	2.838	100.0	
1.779	2*	0.0	0+	1.779	100.0	

Gamma Rays from (n,n' γ) Reactions in ^{28}Si

Initial	State	Final S	State		
Energy (MeV)	J ″	Energy (MeV)	J^{π}	E ⋎ (MeV)	Transition Probability %
6.379	1/2-	2.425	3/2+	3.954	8.0
6.379	$1/2^{-}$	1.273	3/2+	5.106	22.0
6.379	1/2-	0.0	$1/2^{+}$	6.379	70.0
4.933	3/2-	1.273	3/2+	3.660	8.0
4.933	3/2-	0.0	$1/2^{+}$	4.933	92.0
3.623	7/2-	3.067	5/2+	0.556	9.0
3.623	7/2-	2.028	5/2+	1.595	90.0
3.623	7/2-	1.273	3/2+	2.350	1.0
3.067	5/2+	2.028	5/2+	1.039	22.0
3.067	5/2+	1.273	3/2+	1.794	78.0
2.425	3/2+	1.273	3/2+	1.152	12.0
2.425	3/2+	0.0	$1/2^{+}$	2.425	88.0
2.028	5/2+	1.273	3/2+	0.755	5.0
2.028	5/2+	0.0	1/2+	2.028	95.0
1.273	3/2+	0.0	$1/2^{+}$	1.273	100.0

Gamma Rays from (n,n' γ) Reactions in ²⁹Si

TABLE 5

Gamma Rays from (n,n' γ) Reactions in ⁵⁰ S:	Gamma	Rays	from	(n,n'y)	Reactions	in	³⁰ si
--	-------	------	------	---------	-----------	----	------------------

Initial	State	Final S	tate		m ••••
Energy (MeV)	${\tt J}^{{ar \eta}}$	Energy (MeV)	J [#]	EY	Transition Probability %
6.745	1-	0.0	0+	6.745	100.0
5.280	4+	0.0	0+	5.280	100.0
4.830	3+	2.235	2+	2.595	50.0
4.830	3+	0.0	0+	4.830	50.0
4.809	2+	2.235	2+	2.574	50.0
4.809	2+	0.0	0+	4.809	50.0
3.788	0+	2.235	2+	1.553	100.0
3.770	1+	2,235	2+	1.535	60.0
3.770	1+	0.0	0+	3.770	40.0
3.498	2+	2.235	2+	1.263	55.0
3.498	2+	0.0	0+	3.498	45.0
2.235	2+	0.0	0+	2.235	100.0

Ev	I	E initial	
(MeV)	Photons/100 Capture	(MeV)	Target Isotope
10.611	0.3	primary	²⁹ Si
8.474	2.7	primary	²⁸ Si
8.373	0.1	primary	²⁹ Si
7.846	0.15	. ,	
7.201	9.0	primary	²⁸ Si
7.113	0.2	primary	²⁹ Si
7.057	0.1	7.057	²⁸ Si
6.746	1.3	6.746	²⁹ Si
6.446	0.1	primary	²⁸ Si
6.420	0.2	1	
6.381	13.5	6.3810	²⁸ Si
6.047	0.6	primary	² ⁸ Si
5.272	1.0	7.507	²⁹ Si
5.1080	4.1	6.3810	²⁸ Si
4.9350	65.0	4,9350	²⁸ Si
4.8410	0.25	4.8410	²⁸ Si
3.9550	2.0	6.3810	²⁸ Si
3.8650	1.4	primary	²⁹ Si
3.7700	0.2	3.7700	²⁹ Si
3.6620	3.7	4,9340	²⁸ Si
3.5390	69.0	primarv	a8Si
3.1020	1.2	primary	²⁹ Sí
3.054	1.4	primary	³⁰ Si
2.7820	1.6	3.5330	³⁰ Si
2.4460	0.3	3.9330	01
2.4260	2.8	2 4260	3 8 S i
2,2350	1.8	2 2 2 2 5	29 Si
2.2050	0.2	nrimary	30 ₅₁
2.093	2.1	primary	28 Si
2.0280	0.5	2 0280	28 Si
1.8670	0.6	4,934	28 Si
1.794	0.6	3.067	²⁸ Si
1.695	0.1	1,6950	³⁰ Si
1.565	0.4	primary	28Si
1.552	0.3	3.7870	²⁹ Si
1.541	0.5	6.3810	28 Si
1.535	0.3	3.7700	²⁹ Si
1.446	0.7	6.3810	28 S i
1.273	19.0	1,273	28 _{Si}
1,152	0.5	2.426	28 Si
0.752	1.6	0.7520	³⁰ Si

Gamma-Ray Energies and Multiplicities due to Thermal Neutron Capture in Silicon

Optical Model Parameters

$$V(\mathbf{r}) = -V_{R}f(\mathbf{r}, \mathbf{R}_{R}, \mathbf{a}_{R}) + V_{SO} \underline{\sigma} \cdot \underline{\ell} \times_{\pi}^{2} \left(\frac{1}{r}\right) \left(\frac{d}{dr}\right) \left[f(\mathbf{r}, \mathbf{R}_{SO}, \mathbf{a}_{SO})\right] \quad \text{Real Part}$$

$$W(\mathbf{r}) = -W_{V} f(\mathbf{r}, \mathbf{R}'_{I}, \mathbf{a}'_{I}) + W_{SF} 4\mathbf{a}_{I} \left(\frac{d}{dr}\right) \left[f(\mathbf{f}, \mathbf{R}_{I}, \mathbf{a}_{I})\right] \quad \text{Imaginary Part}$$

where $f(r,R,a) = \frac{1}{1 + e^{(r-R)/a}}$

- $\underline{\sigma}$: $\underline{\ell}$ = scalar product of intrinsic and orbital angular momentum operators.
- λ_{π}^{2} = pion Compton wave-length squared $\simeq 2.0 \text{ fm}^{2}$. A = target mass number.

All radii of the form: $R_I = r_I A^{1/3}$.

$$V_{\rm R}$$
 = 56.3 - 0.32E - 24.0 $\frac{(\rm N-Z)}{\rm A}$

$$r_R = 1.17 a_R = 0.75$$

 $W_V = 0$
 $W_{SF} = 13.0 - 0.25E - 12.0 \frac{(N-Z)}{A}$ or zero, whichever is greater.
 $r_I = r_{I'} = 1.26 a_I = a_{I'} = 0.58$

 $V_{SO} = 6.2$ $r_{SO} = 1.01$ $a_{SO} = 0.75$ where E is the incident neutron lab energy in MeV.

Leve1	Dens	sity	r Par	ameters	of	the	Isotopes
ι	Jsed	in	the	Cascade	Cal	Lcu1a	ations*

	а	Т	Eo	Ex	σ	δ
^{a9} Si	3.57	1.91	0.75	8.1	2.1	2.09
²⁸ Si	3.05	2.09	3.20	12.9	2.0	3.89
27Si	2.6	1.91		8.1	2.0	2.09
3 8 A L	3.65	1.50	-0.70	6.8	2.2	0
27AL	3.45	2.08	-0.35	9.6	2.0	1.80
₽7 _{Mg}	4.0	2.04	-0.80	12.2	2.25	2.46
a 5 Mg	3.85	2.12	-1.00	12.4	2.15	2.46
²⁴Mg	3.32	2.18	2.80	13.0	2.0	5.31

*where a = level density parameters (MeV⁻¹), T = temperature of nuclei (MeV), E_o = normalization energy (MeV), E_x = energy of tangency point (MeV), σ = spin cut-off parameter; δ = pairing energy (MeV).

σ
TABLE

Yrast Levels of Nuclei Produced by Cascade Processes in $^{2\,\mathrm{B}}\mathrm{Si}$ Neutron Reactions

Ne	4	0	.347	.75	122	864	462	.164	164	.626	e.	0	17
ิณิ	5	0	С		4	8	12	15	18	21	25	29	33
²⁴ Na	0.5633	3.37	0.0	3.8	3.22	7.633	9.685	12.078	14.814	17.892	21.312	25.07	29.18
²⁴ Mg	0.0	7.561	1.368	5.228	4.122	8.864	12.462	15.109	18.164	21.626	25.3	29.0	33.17
²⁵ Mg	0.5852	0.9747	0.	1.6137	3.400	7.633	9.685	12.078	14.814	17.892	21.312	25.074	29.178
²^Mg	0.0	0.984	1.692	3.757	5.757	7.633	9.685	12.078	14.814	17.892	21.312	25.074	29.10
27Al	0.842	1.013	0.	2.209	3.000	7.287	9.464	12.003	14.905	18.170	21.798	25.25	29.10
28Al	6.0	1.372	0.030	0.0	2.207	2.49	6.025	8.201	10.711	13.556	16.736	20.251	24.10
a7Si	0.780	0.953	0.0	2.165	5.472	7.143	9.147	11.486	14.158	17.165	20.505	24.18	28.19
²⁸ Si	0.0	7.382	1.778	6.690	4.614	8.897	11.10	13.704	16.708	20.113	23.50	27.18	31.19
2 ⁹ Si	0.	1.273	2.0	3.623	5.472	7.143	9.147	11.486	14.158	17.165	20.505	24.18	28.19
Spin	0 or 1/2	1	2	e	4	5	9	7	8	6	10	11	12

Binding Energies of Neutron, Proton, and α -Particles for Nuclei Produced by Cascade Processes in ²⁸Si Neutron Reactions (MeV)

²⁹ Si		²⁹ Si ²⁸ Si		⁸ Si	²⁷ Si		2	[₿] Aℓ	²⁷ Al		
n	²⁸ Si	8.475	²⁷ Si	17.175	²⁶ Si	13.32	27Al	7.731	2°Al	13.057	
р	3 8 A L	12.327	27AL	11.583	26AL	7.464	27Mg	9.562	°°Mg	8.271	
α	^{≈5} Mg	11.128	²⁴Mg	9.981	²³ Mg	9.338	²⁴ Na	10.862	²³ Na	10.093	

	5	⁵ Mg	2	⁴ Mg	3.	⁴ Na	al _{Ne*}		
n	²⁴ Mg	7.329	²³Mg	16.532	²³ Na	6.961	² [∩] Ne	6.759	
р	²⁴ Na	12.061	^{₂з} Na	11.694	²³ Na	10.599	₽°F	13.007	
α	'¹Ne	9.886	[≈] °Ne	9.317	²⁰ Fe	10.83	170	7.347	



Figure 1



Figure 2



Figure 3



-36-



-37-



Figure 8







-40-



Figure 13



Figure 14



Figure 15



Figure 16



Figure 17



Figure 18







ENERGY-EV



-49-





Figure 31



120

ióo

15

20

140







Figure 37



Figure 38









Figure 34



Figure 35

Figure 39

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